

$$7. \quad 9y^2 - 4x^2 + 18y + 40x - 127 = 0$$

$$9y^2 + 18y - 4x^2 + 40x = 127$$

$$9(y^2 + 2y) - 4(x^2 - 10x) = 127$$

$$9(\underbrace{y^2 + 2y + 1}_{(y+1)^2}) - 4(\underbrace{x^2 - 10x + 25}_{(x-5)^2} - 25) = 127$$

$$9(y^2 + 2y + 1) + 9(-1) - 4(x^2 - 10x + 25) - 4(-25) = 127$$

$$9(\underline{y+1})^2 - 9 - 4(\underline{x-5})^2 + 100 = 127$$

$$9(y+1)^2 - 4(x-5)^2 = 127 - 100 + 9$$

$$9(y+1)^2 - 4(x-5)^2 = 36$$

$$\frac{9(y+1)^2}{36} - \frac{4(x-5)^2}{36} = \frac{36}{36}$$

$$\frac{(y+1)^2}{4} - \frac{(x-5)^2}{9} = 1$$

$$\begin{array}{l} k = -1 \\ \frac{(y+1)^2}{(2)^2} - \frac{(x-5)^2}{(3)^2} = 1 \\ \downarrow \\ a = 2 \\ \downarrow \\ b = 3 \end{array}$$

WRITING IN STANDARD FORM

① GROUP X'S, GROUP Y'S, TAKE NUMBER TO RIGHT SIDE

② FACTOR OUT THE NUMBER IN FRONT OF SQUARES

③ COMPLETE THE SQUARE ON Y'S AND ON THE X'S

Y'S	X'S
$(2 \cdot \frac{1}{2})^2$	$(-10 \cdot \frac{1}{2})^2$
$(1)^2$	$(-5)^2$
1	25

④ GET A "ONE" ON RIGHT SIDE

RIGHT

FIND C

$$b^2 = c^2 - a^2$$

$$3^2 = c^2 - 2^2$$

$$9 = c^2 - 4$$

$$9 + 4 = c^2$$

$$13 = c^2$$

$$c = \sqrt{13}$$