

$$0 \leq x < 2\pi$$

7.  $f(x) = 2\sin x - 2\cos x$

①  $f'(x) = 2\cos x - 2(-\sin x)$

$$= 2\cos x + 2\sin x$$

$f''(x) = 2(-\sin x) + 2\cos x$

$$= -2\sin x + 2\cos x$$

②  $-2\sin x + 2\cos x = 0$

$$2\cos x = 2\sin x$$

$$\cos x = \sin x$$

$$\cos^2 x = \sin^2 x$$

$$1 - \sin^2 x = \sin^2 x$$

$$1 = 2\sin^2 x$$

$$1 = 2\sin^2 x$$

$$\frac{1}{2} = \sin^2 x$$

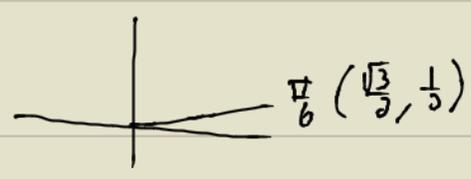
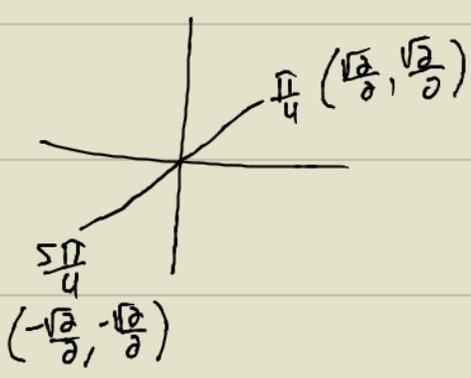
$$\pm \sqrt{\frac{1}{2}} = \sin x$$

$$\sin x = \pm \frac{\sqrt{2}}{2}$$

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$$x = \left(\frac{\pi}{4}\right), \frac{3\pi}{4}, \left(\frac{5\pi}{4}\right), \frac{7\pi}{4}$$

BY INSPECTION



③

$x=0$        $x=\frac{\pi}{4}$        $x=\frac{5\pi}{4}$        $x=2\pi$

$x = \frac{\pi}{6}$	$x = \pi$	$x = \frac{3\pi}{2}$
$-2\sin x + 2\cos x$	$-2\sin x + 2\cos x$	$-2\sin x + 2\cos x$
$-2\sin \frac{\pi}{6} + 2\cos \frac{\pi}{6}$	$-2\sin \pi + 2\cos \pi$	$2 + 0$
$-1 + \frac{\sqrt{3}}{2}$	NEG	POS
NEG		

CONC DOWN  $(0, \frac{\pi}{4})$   
 CONC DOWN  $(\frac{\pi}{4}, \frac{5\pi}{4})$   
 CONC UP  $(\frac{5\pi}{4}, 2\pi)$

④ POI AT  $x = \frac{5\pi}{4}$

$$f\left(\frac{5\pi}{4}\right) = 2\sin \frac{5\pi}{4} - 2\cos \frac{5\pi}{4}$$

$$= 2\left(-\frac{\sqrt{2}}{2}\right) - 2\left(-\frac{\sqrt{2}}{2}\right)$$

$$= -\sqrt{2} + \sqrt{2} = 0$$

POI  $\left(\frac{5\pi}{4}, 0\right)$