

$$15. \int \frac{x}{\sqrt{4+10x^2-x^4}} dx$$

$$= \int \frac{x}{\sqrt{-x^4+10x^2+4}} dx$$

$$\left(-10 \cdot \frac{1}{2}\right)^2$$

$$= \int \frac{x}{\sqrt{-(x^4-10x^2-4)}} dx$$

$$\frac{(-5)^2}{25}$$

$$= \int \frac{x}{\sqrt{-(x^4-10x^2+25-25-4)}} dx$$

$$= \int \frac{x}{\sqrt{-[(x^2-5)^2-29]}} dx$$

$$= \int \frac{x}{\sqrt{29-(x^2-5)^2}} dx$$

$$= \int \frac{x}{\sqrt{(\sqrt{29})^2-(x^2-5)^2}} dx$$

$$a = \sqrt{29} \quad u = x^2 - 5 \quad du = 2x dx$$

$$= \frac{1}{2} \int \frac{2x}{\sqrt{(\sqrt{29})^2-(x^2-5)^2}} dx$$

$$= \frac{1}{2} \int \frac{1}{\sqrt{a^2-u^2}} du$$

$$= \frac{1}{2} \cdot \arcsin \frac{u}{a} + C$$

$$= \frac{1}{2} \arcsin \frac{x^2-5}{\sqrt{29}} + C$$