

EQUALITY OF EXPONENTS

IF

$$b^P = b^Q$$

THEN

$$P = Q$$

1. $2^X = 16$

$$2^X = 2^4$$

$$\boxed{X=4}$$

2. $3^{X-5} = 27$

$$3^{X-5} = 3^3$$

$$X-5=3$$

$$X=3+5$$

$$\boxed{X=8}$$

3. $\left(\frac{1}{4}\right)^{5X-1} = 8$

$$\left(\frac{1}{2^2}\right)^{5X-1} = 2^3$$

$$(2^{-2})^{5X-1} = 2^3$$

$$-10X+2 = 3$$

$$-10X = 3-2$$

$$-10X = 1$$

$$-10X = 1$$

$$\frac{-10X}{-10} = \frac{1}{-10}$$

$$\boxed{X = -\frac{1}{10}}$$

POWER PRINCIPLE

IF

$$P = Q$$

THEN

$$P^n = Q^n$$

IF FRACTIONAL EXPONENT

IF

$$P^{\frac{a}{b}} = Q$$

$$P = Q^{\frac{b}{a}}$$

IF a IS EVEN

PUT \pm BEFORE Q

4. $X^{\frac{3}{4}} = 27$ ← ODD, so no \pm

$$\left(X^{\frac{3}{4}}\right)^{\frac{4}{3}} = 27^{\frac{4}{3}}$$

$$X = \left(27^{\frac{1}{3}}\right)^4$$

$$X = \left(\sqrt[3]{27}\right)^4$$

$$X = \left(\sqrt[3]{3 \cdot 3 \cdot 3}\right)^4$$

$$X = 3^4$$

$$\boxed{X=81}$$

5. $X^{\frac{2}{3}} = 16$ ← EVEN, so put \pm

$$\left(X^{\frac{2}{3}}\right)^{\frac{3}{2}} = \pm 16^{\frac{3}{2}}$$

$$X = \pm \left(16^{\frac{1}{2}}\right)^3$$

$$X = \pm \left(\sqrt{16}\right)^3$$

$$X = \pm 4^3$$

$$\boxed{X = \pm 64}$$