

$$4. f(x) = \frac{7}{(x^2-9)^3}$$

$$= 7(x^2-9)^{-3}$$

$$f'(x) = 7(-3)(x^2-9)^{-3-1} \cdot \frac{d}{dx}(x^2-9)$$

$$= -21(x^2-9)^{-4} \cdot (2x)$$

$$= \frac{-42x}{(x^2-9)^4}$$

$$5. f(x) = \underbrace{x^5}_P \underbrace{(x-7)^8}_Q$$

$$P' = 5x^4 \quad Q' = 8(x-7)^7 \cdot \frac{d}{dx}(x-7)$$

$$= 8(x-7)^7 \cdot 1$$

$$= 8(x-7)^7$$

$$P'Q + PQ'$$

$$f'(x) = \underbrace{5x^4(x-7)^8} + \underbrace{x^5 \cdot 8(x-7)^7}$$

$$= x^4(x-7)^7 [5(x-7) + x]$$

$$= x^4(x-7)^7 [5x - 35 + x]$$

$$= x^4(x-7)^7 (6x - 35)$$

$$= \boxed{x^4(6x-35)(x-7)^7}$$