

3. $f(x) = X\sqrt{x+a}$

① Domain: $x+a \geq 0$
 $x \geq -a$

② $x=0$: $0 = X\sqrt{x+a}$
 $x=0$ $\sqrt{x+a}=0$
 $x+a=0$
 $x=-a$

③ $y=0$: $y=0\sqrt{0+a}$
 $y=0$

- ④ VA: NONE
- ⑤ HA: NONE
- ⑥ SA: NONE

⑦ $f(x) = \underbrace{x}_{P}(\underbrace{x+a}_{Q})^{\frac{1}{2}}$

$P'=1$ $Q' = \frac{1}{2}(x+a)^{-\frac{1}{2}} \cdot \frac{d}{dx}(x+a)$
 $= \frac{1}{2(x+a)^{\frac{1}{2}}}$

$P'Q + PQ'$

$f'(x) = 1(x+a)^{\frac{1}{2}} + x\left(\frac{1}{2(x+a)^{\frac{1}{2}}}\right)$

$= \frac{(x+a)^{\frac{1}{2}}}{1} + \frac{x}{2(x+a)^{\frac{1}{2}}}$

$= \frac{(x+a)^{\frac{1}{2}} \cdot 2(x+a)^{\frac{1}{2}}}{2(x+a)^{\frac{1}{2}} \cdot 2(x+a)^{\frac{1}{2}}} + \frac{x}{2(x+a)^{\frac{1}{2}}}$

$= \frac{2(x+a)^{\frac{1}{2}} \cdot 2(x+a)^{\frac{1}{2}}}{2(x+a)^{\frac{1}{2}} \cdot 2(x+a)^{\frac{1}{2}}} + \frac{x}{2(x+a)^{\frac{1}{2}}}$

$= \frac{2(x+a) + x}{2(x+a)^{\frac{1}{2}}}$

$= \frac{2x + 4 + x}{2(x+a)^{\frac{1}{2}}}$

* $f'(x) = \frac{(3x+4)}{2(x+a)^{\frac{1}{2}}}$

$3x+4=0$
 $3x=-4$
 $x = -\frac{4}{3}$

$2(x+a)^{\frac{1}{2}}=0$
 $x+a=0$
 $x=-a$

DEC $(-a, -\frac{4}{3})$
 INC $(-\frac{4}{3}, \infty)$

$x = -3$ ERR	$x = -\frac{5}{3}$ NEC	$x = 0$ ms	t.c. plug into $f'(x)$
	\	/	
	MIN		

⑧ RELATIVE EXTREMA
 REL MIN $(-\frac{4}{3}, -1.1)$