

$$9. f(x) = \underbrace{(5+3x)}_P \underbrace{e^{-4x}}_Q$$

$$P' = 3 \quad Q' = e^{-4x} \cdot \frac{d}{dx}(-4x) \\ = e^{-4x} \cdot (-4)$$

$$Q' = -4e^{-4x}$$

$$P'Q + PQ'$$

$$f'(x) = 3e^{-4x} + (5+3x) \cdot (-4e^{-4x})$$

$$= e^{-4x} [3 + (5+3x)(-4)]$$

$$= e^{-4x} (3 - 20 - 12x)$$

$$= e^{-4x} (-12x - 17)$$

$$f''(x) = \underbrace{-e^{-4x}}_P \underbrace{(12x+17)}_Q$$

$$P' = -e^{-4x} \cdot \frac{d}{dx}(-4x) \quad Q' = 12$$

$$= -(-4)e^{-4x}$$

$$P' = 4e^{-4x}$$

$$P'Q + PQ'$$

$$f''(x) = 4e^{-4x} (12x+17) + (-e^{-4x})(12)$$

$$= 4e^{-4x} [12x+17-3]$$

$$= 4e^{-4x} (12x+14)$$

$$= 4 \cdot 2 e^{-4x} (6x+7)$$

$$= \boxed{8e^{-4x} (6x+7)}$$