

$$10. f(x) = x^3 e^{-x}$$

① Domain

$$f(x) = \frac{x^3}{e^x}$$

$$e^x = 0$$

$$\cancel{LNE^x = LNO}$$

$$(-\infty, \infty)$$

② X-INT

$$0 = x^3 e^{-x}$$

$$x^3 = 0 \quad \cancel{e^{-x} = 0}$$

$$x = 0$$

③

Y-INT

$$y = 0^3 e^{-0}$$

$$y = 0(1)$$

$$y = 0$$

④ V.A.

NONE

⑤ H.A.

$$\lim_{x \rightarrow \infty} x^3 e^{-x}$$

$$= \lim_{x \rightarrow \infty} \frac{x^3}{e^x}$$

L'Hôpital's Rule

$$= \lim_{x \rightarrow \infty} \frac{3x^2}{e^x}$$

$$= \lim_{x \rightarrow \infty} \frac{6x}{e^x}$$

$$= \lim_{x \rightarrow \infty} \frac{6}{e^x}$$

$$= \frac{6}{e^\infty}$$

$$= \frac{6}{\infty}$$

$$= 0$$

⑥ S.A.

NONE

H.A.

$$y = 0$$