

10. (cont.)

$$y' = 3x^2 e^{-x} - x^3 e^{-x}$$
$$= \underbrace{e^{-x}}_P \underbrace{(3x^2 - x^3)}_Q$$

$$P' = e^{-x} \cdot \frac{d}{dx}(-x)$$

$$P' = -e^{-x} \quad Q' = 6x - 3x^2$$

$$P'Q + P Q'$$

$$y'' = -e^{-x}(3x^2 - x^3) + e^{-x}(6x - 3x^2)$$

$$= e^{-x}(-3x^2 + x^3 + 6x - 3x^2)$$

$$= e^{-x}(x^3 - 6x^2 + 6x)$$

$$y'' = x e^{-x}(x^2 - 6x + 6)$$

$$x=0 \quad \cancel{e^{-x}=0} \quad x^2 - 6x + 6 = 0$$

$$a=1 \quad b=-6 \quad c=6$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(6)}}{2(1)}$$

$$= \frac{6 \pm \sqrt{36 - 24}}{2}$$

$$= \frac{6 \pm \sqrt{12}}{2}$$

$$= \frac{6 \pm 2\sqrt{3}}{2}$$

$$= 3 \pm \sqrt{3}$$

4.7, 1.3