

$$1. f(x) = x^2 + x - 1$$

$$\frac{dy}{dx} = 2x + 1$$

$$dx \left(\frac{dy}{dx} \right) = (2x + 1) dx$$

$$dy = (2x + 1) dx$$

$$dy = (2 \cdot 1 + 1) \cdot 0.01$$

$$= 3(0.01)$$

$$= \boxed{0.03}$$

$$\Delta y = f(x + \Delta x) - f(x)$$

$$\Delta y = f(1 + 0.01) - f(1)$$

$$= f(1.01) - f(1)$$

$$= (1.01)^2 + (1.01) - 1 - (1^2 + 1 - 1)$$

$$= 1.0201 + 0.01 - 1$$

$$= 1.0301 - 1$$

$$= \boxed{0.0301}$$

$$2. f(x) = x^{-\frac{1}{2}} = \frac{1}{x^{\frac{1}{2}}} = \frac{1}{\sqrt{x}} \quad \Delta y = f(x + \Delta x) - f(x)$$

$$\frac{dy}{dx} = -\frac{1}{2} x^{-\frac{3}{2}}$$

$$= f(1 + \Delta x) - f(1)$$

$$dy = \left(\frac{-1}{2x^{\frac{3}{2}}} \right) dx$$

$$= \frac{1}{\sqrt{1 + \Delta x}} - \frac{1}{\sqrt{1}}$$

$$= \left(\frac{-1}{2 \cdot 1^{\frac{3}{2}}} \right) dx$$

$$\Delta y = \frac{1}{\sqrt{1 + \Delta x}} - 1$$

$$dy = -\frac{1}{2} dx$$

2