

$$10. f(x) = \frac{x^2}{x^2-5} \quad \text{P} \quad \text{Q} \quad [-2, 4]$$

$$① \quad f' = 2x \quad Q' = 2x$$

$$\frac{P'Q - PQ'}{Q^2}$$

$$f'(x) = \frac{2x(x^2-5) - x^2(2x)}{(x^2-5)^2}$$

$$= \frac{2x[x^2-5-x^2]}{(x^2-5)^2}$$

$$f'(x) = \frac{-10x}{(x^2-5)^2}$$

②

$$-10x = 0$$

$$x = 0$$

$$(x^2-5)^2 = 0$$

$$x^2-5 = 0$$

$$x^2 = 5$$

$$x = \pm\sqrt{5}$$

$$x = -\sqrt{5} \quad x = \sqrt{5}$$

③

$$x = -2$$

$$y = \frac{x^2}{x^2-5}$$

$$y = \frac{(-2)^2}{(-2)^2-5}$$

$$= \frac{4}{4-5}$$

$$= \frac{4}{-1}$$

$$y = -4$$

$$x = 0$$

$$y = \frac{x^2}{x^2-5}$$

$$y = \frac{0^2}{0^2-5}$$

$$y = 0$$

~~$$x = \sqrt{5}$$~~

~~$$y = \frac{x^2}{x^2-5}$$~~

~~$$y = \frac{(\sqrt{5})^2}{(\sqrt{5})^2-5}$$~~

~~$$= \frac{5}{5-5}$$~~

~~$$= \text{undefined}$$~~

$$x = 4$$

$$y = \frac{x^2}{x^2-5}$$

$$y = \frac{4^2}{4^2-5}$$

$$= \frac{16}{16-5}$$

$$= \frac{16}{11}$$

Abs. min:  $(-2, -4)$

Abs. max:  $(4, \frac{16}{11})$