

$$11. \int x \sqrt{x^2 - 8} \, dx$$

$$u = x^2 - 8 \quad du = (2x) \, dx$$

$$= \frac{1}{2} \int \frac{2x}{2} \sqrt{x^2 - 8} \, dx$$

$$= \frac{1}{2} \int \sqrt{u} \, du$$

$$= \frac{1}{2} \int u^{\frac{1}{2}} \, du$$

$$= \frac{1}{2} \cdot \frac{u^{\frac{1}{2}+1}}{\frac{1}{2}+1} + C$$

$$= \frac{1}{2} \cdot \frac{u^{\frac{3}{2}}}{\frac{3}{2}} + C$$

$$= \frac{1}{2} \cdot \frac{2}{3} u^{\frac{3}{2}} + C$$

$$= \frac{1}{3} (x^2 - 8)^{\frac{3}{2}} + C$$

$$12. \frac{dQ}{dx} = \frac{0.94}{(x - 24999)^{0.06}}, \quad x \geq 25000$$

$$Q = \int \frac{dQ}{dx}$$

$$Q = \int \frac{0.94}{(x - 24999)^{0.06}} \, dx$$

$$Q = 0.94 \int \frac{1}{(x - 24999)^{0.06}} \, dx$$

$$u = x - 24999 \quad du = 1 \cdot dx$$

$$dx = du$$

$$Q = 0.94 \int \frac{1}{u^{0.06}} \, du$$

$$Q = 0.94 \int u^{-0.06} \, du$$

$$Q = 0.94 \cdot \frac{u^{-0.06+1}}{-0.06+1} + C$$

$$Q = 0.94 \cdot \frac{(x - 24999)^{.94}}{.94} + C$$

$$Q = (x - 24999)^{.94} + C$$

$$25000 = (25000 - 24999)^{.94} + C$$

$$25000 = 1^{.94} + C$$

$$25000 = 1 + C$$

$$C = 24999$$

$$24999 = C$$

$$Q = (x - 24999)^{.94} + 24999$$