

Asymptotes

In problems 1-4, Find the vertical and horizontal asymptotes.

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| 1. $f(x) = \frac{3x^2 - 7x + 1}{4x^2 - 16}$ | 2. $f(x) = \frac{x^2 - 2x - 3}{x^2 - 9}$ |
| 3. $f(x) = \frac{2x}{x^2 - 12x + 20}$ | 4. $f(x) = \frac{x^2 + 8x + 2}{x - 3}$ |

In problems 5-7, Find the vertical asymptote(s)

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| 5. $f(x) = \frac{3}{7x^2 + 13x - 2}$ | 6. $f(x) = \frac{x^2 - 4x - 21}{x^2 - 49}$ |
| 7. $f(x) = \frac{x^2 + 8x + 15}{x^2 - 2x - 35}$ | |

In problems 8-10, Use the TI-83/84 to find the limit

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| 8. $\lim_{x \rightarrow 5^+} \frac{x-1}{x-5}$ | 9. $\lim_{x \rightarrow 3^-} \frac{2}{(x-3)^2}$ |
| 10. $\lim_{x \rightarrow 2^-} \frac{x^2 - 3}{x^2 - 4}$ | |

In problems 11-12, Find the limit

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| 11. $\lim_{x \rightarrow \infty} \left(2 + \frac{5}{x} \right)$ | 12. $\lim_{x \rightarrow \infty} \left(3 + \frac{1}{x^2} \right)$ |
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In problems 13-17, Find the horizontal asymptotes.

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| 13. $f(x) = \frac{7x + 2}{5x - 1}$ | 14. $f(x) = \frac{3x^2 - 4x + 1}{8x + 3}$ |
| 15. $f(x) = \frac{8x + 1}{x^2 - 5x + 1}$ | 16. $f(x) = \frac{4x^2 + 3x - 5}{2x^2 - x + 3}$ |
| 17. $f(x) = \frac{3}{x^2 - 5x + 1}$ | |

Asymptotes

In problem 18, Find each limit

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| 18. a) $\lim_{x \rightarrow \infty} \frac{x^2 + 3}{x^3 - x + 2}$ b) $\lim_{x \rightarrow \infty} \frac{3x^2 + 1}{4x^2 - 3x + 5}$ c) $\lim_{x \rightarrow \infty} \frac{x^3}{x^2 - 5 + 1}$ | |
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In problems 19-22, sketch the graph of the equation. Use intercepts, extrema, and asymptotes.

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| 19. $f(x) = \frac{x+1}{x-2}$ | 20. $f(x) = \frac{3x^2 + 1}{x^2 - 4}$ |
| 21. $f(x) = \frac{x^2 - 5x + 2}{x+1}$ | 22. $f(x) = \frac{7x-1}{x^2 - 9}$ |