

VARIATION

20000 40000
30000 60000

$$F = 2D$$

↑
(K)
CONSTANT OF
PROPORTIONALITY

$$\text{HAPPINESS} = \frac{(\text{CIRCUS})(\text{SON})}{(\text{FRANCS})}$$

SOLVING VARIATION PROBLEMS

1. DETERMINE TYPE
 - DIRECT : $y = kx$
 - INVERSE : $y = \frac{k}{x}$
 - JOINT : $y = kxz$
 - COMBO : MIX OF ABOVE
2. PICK VARIABLES THAT MAKE SENSE
3. LOOK FOR ONE EXAMPLE AND SOLVE FOR K
4. FIND WHAT THEY REALLY WANT

#1

① DIRECT : $y = kx$

② $y = kx$

③ $25 = k(5)$

$$\frac{25}{5} = \frac{5k}{5}$$

$$5 = k$$

$$y = 5x$$

④ $y = 5(7)$

$$y = 35$$

#2

① INVERSE : $y = \frac{k}{x}$

② $y = \frac{k}{x}$

③ $8 = \frac{k}{20}$

$$2(20) = \frac{k(20)}{20}$$

$$160 = k$$

$$y = \frac{160}{x}$$

④ $y = \frac{160}{35}$

$$y = \frac{32}{7}$$

#3

① JOINT : $y = kxz$

② $y = kxz$

③ $30 = k(4)(3)$

$$30 = 12k$$

$$\frac{30}{12} = k$$

$$\frac{5}{2} = k$$

$$y = \frac{5}{2}(xz)$$

④ $y = \frac{5}{2}(10)(7)$

$$y = 175$$

$$\begin{array}{r} 3 \\ 25 \\ \hline 175 \end{array}$$

#4

① DIRECT : $y = kx$

② $P = kn$

③ $4131 = k(810)$

$$\frac{4131}{810} = k$$

$$5.1 = k$$

$$P = 5.1n$$

④ $P = 5.1(520)$

$$P = 2652$$

#5

① INVERSE : $y = \frac{k}{x}$

② $A = \frac{k}{D^2}$

③ $13.1 = \frac{k}{10.2^2}$

$$13.1 = \frac{k}{104.04}$$

$$13.1(104.04) = k$$

$$1362.924 = k$$

$$A = \frac{1362.924}{D^2}$$

④

$$A = \frac{1362.924}{27.5^2}$$

$$A = 1.8$$